

# Key ingredient

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## KEY INGREDIENTS TO DEVELOP AN 'APPROPRIATE' INNOVATION

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### **Abstract**

Improving educational achievement of a particular country cannot be simply done by applying other countries' systems<sup>4</sup>. This paper describes how improving educational performance should be done on the basis of the specific needs and the existing educational practice of a particular country. For this purpose, two aspects are discussed: error analysis and opportunity-to-learn. Examples from a so called CoMTI (Context-based Mathematics Tasks Indonesia) Project were provided to show how these two aspects serve as important bases to develop ways to improve Indonesian students' performance on context-based mathematics tasks.

**Keywords:** educational achievement; error analysis; opportunity-to-learn

### **INTRODUCTION**

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The result of international comparative tests – such as the Programme for International Student Assessment (PISA) and the Trends in International Mathematics and Science Studies (TIMSS) – is considered as an important educational benchmark. This situation has led many countries to improve their educational achievement, for which various ways have been applied in different countries. For example, Finland attributes its success in education to teacher quality, whereas Singapore and the Netherlands point to their curriculum (Stacey, 2011). Another way is used by Japan that refers its success in education to carefully constructed lessons and its culture of lesson study. Reflecting upon these different ways for improving educational achievement, we might question: “*what is the best way to improve educational achievement?*” It is not easy to answer this question because, according to Pearson (2014) and Stacey (2011), what works in one particular country will not necessarily give the same result in other countries. A new question, then, arises: “*how can we develop an appropriate way to improve educational achievement of a particular country?*”

The educational achievement of a country could be improved through an innovation. However, an innovation does not simply mean applying other countries' educational practices. Regarding this issue, this paper describes how improving students'

performance of a particular country should be done <sup>4</sup> on the basis of the needs and the existing educational practice of that country. This is what it means to be an appropriate innovation. For this purpose, error analysis and opportunity-to-learn are considered as the key aspects. As illustrative examples, some results of CoMTI (Context-based Mathematics Tasks Indonesia) Project<sup>2</sup> (Wijaya, 2015) are provided.

### **Error Analysis: A Preliminary Step to Improve Students' Performance**

Scores resulted from a particular test (e.g. PISA and TIMSS) indeed give an indication of students' performance. However, scores do not provide enough information to improve students' performance. In order to develop appropriate way(s) to improve students' performance, we need detailed information on specific difficulties encountered by students. Investigating students' difficulties is a crucial step in the process of improving student performance because it sheds light on specific aspects or competences that need to be developed. Students' difficulties can be investigated through an error analysis because students' errors are considered as a powerful source to diagnose learning difficulties (Brodie, 2014; Radatz, 1980). Students' errors illustrate the difficulties experienced by students, provide access to students' reasoning, and provide information on students' understanding of certain concepts or procedures. Such information cannot be obtained if we rely only on students' scores. According to Radatz, error analysis has a crucial role both in academic practice and in research. In academic practice error analysis is an important means to diagnose students' learning difficulties, to develop criteria for differentiated learning, and to create support for students' performance and understanding. In terms of research, error analysis is a remarkable starting point for research on mathematical teaching and learning because it can clarify fundamental questions of mathematics learning.

A key aspect of error analysis is developing analysis framework as a direction to identify students' errors, which, later, leads to an investigation of students' difficulties. An analysis framework can be derived from a theoretical perspective, developed on the basis of students' actual work for which we can refer to a so called 'grounded theory', or a combination of both ways. An example of framework that <sup>5</sup> uses the combination of both ways is the framework analysis that was developed by Wijaya, Van den Heuvel-Panhuizen, Doorman, and Robitzsch (2014) to identify students' errors in solving context-based mathematics tasks. The four error types – comprehension, transformation, mathematical processing, and encoding – in this framework were derived from theoretical perspective by considering Blum's (2011) modeling process and PISA's (OECD, 2003) mathematization, whereas the sub-types of each error type were developed on the basis of students' work.

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<sup>2</sup> CoMTI project is <sup>2</sup> PhD research of Ariyadi Wijaya under the supervision of Marja van den Heuvel-Panhuizen and Michiel Doorman from Freudenthal Institute, Utrecht University, the Netherlands. The aim of this project was to identify way(s) to improve Indonesian students' performance on context-based tasks.

### **Opportunity-to-learn: A bridge between students' learning difficulties and appropriate innovation at classrooms**

McKinsey (2010) points out that the best approach or resource to improve an educational practice depends greatly on the existing condition of that practice. In relation to improving students' performance, we need to investigate the existing educational practice and connect it to the needs and/or the learning difficulties of students. For this purpose, we can consider a so called 'opportunity-to-learn' that is often used to find an explanation for students' mathematics performance. In the First International Mathematics Study opportunity-to-learn was defined as "whether or not [...] students have had the opportunity to study a particular topic or learn how to solve a particular type of problem" (Husén, 1967, p. 162-163). Opportunity-to-learn, according to Brewer and Stasz (1996), can be measured from three interrelated dimensions. The first dimension is curriculum content that refers to the scope of the topics offered to students. The second dimension is instructional resources, such as textbooks, which are used to teach students. The third dimension is instructional strategies, i.e. teaching strategies that are used by teachers to present the topics and to engage students.

In terms of research at school level, we can focus on the second and the third dimension: instructional resources and instructional strategies. Research has shown that textbooks have a strong influence on students' learning. The degree of exposure to particular content included in a textbook can influence students' performance. Tornroos (2005) found a relation between student achievement on a test and the amount of textbook content related to the test items. The characteristics of tasks in textbooks can also determine students' opportunity to learn. A task that emphasizes on routine procedure might only develop students' procedural knowledge and skills, but, on the other hand, a task with implicit procedure might develop students' ability to make a mathematical model. With respect to the dimension of instructional strategies, several studies (e.g. Hiebert & Grouws, 2007) revealed that students' mathematical performance is largely influenced by teachers' teaching practices. The strategies used by teachers to teach particular topics, the kind of tasks provided by teachers, and the nature of the discussions they organized in class are important factors influencing students' opportunity-to-learn. Therefore, investigating the current teaching practices is important to identify whether that practice fit the targeted goals or competences.

#### **An Example from CoMTI project**

As an illustrative example how error analysis and an investigation into students' opportunity-to-learn can be used as the basis for developing way(s) to improve students' performance, I provide some results of CoMTI project.

As their first attempt to improve Indonesian students' performance on context-based tasks, Wijaya et al. (2014) investigated students' difficulties when solving such tasks through an error analysis. They identified four types of errors made by (Indonesian) students when solving context-based tasks, i.e. *comprehension* (error in understanding the meaning of a problem), *transformation* (error in transforming a word problem into a



mathematical problem), *process skills* (error in performing mathematical procedures), and encoding (error in interpreting the mathematical solution). Among these error types, comprehension and transformation errors were found to be the most dominant errors made by the students, i.e. 38% and 42%, respectively. These results indicate that improving (Indonesian) students' performance on context-based tasks can be done by enhancing students' ability to comprehend a context-based task and to transform it into a mathematical problem. A closer examination into students' errors revealed that a half of the comprehension errors were errors in selecting relevant information. This finding suggests that improving the task comprehension of Indonesian students requires a focus not only on students' language competence, but also on the ability to select relevant information.

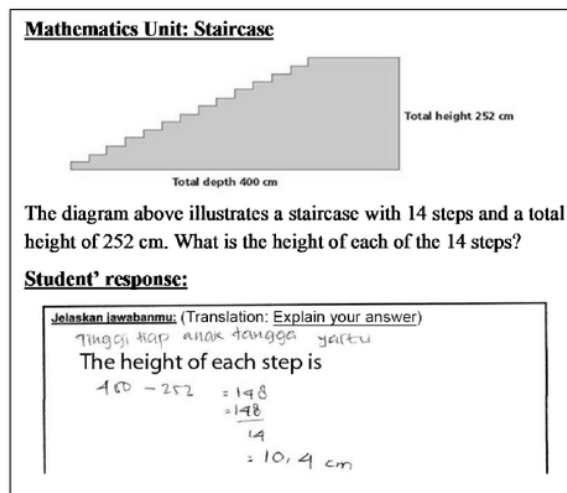


Figure 1. An example of *comprehension error*, in particular *error in selecting information*

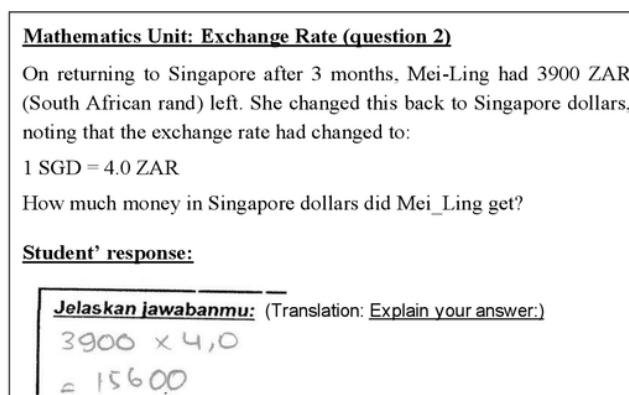
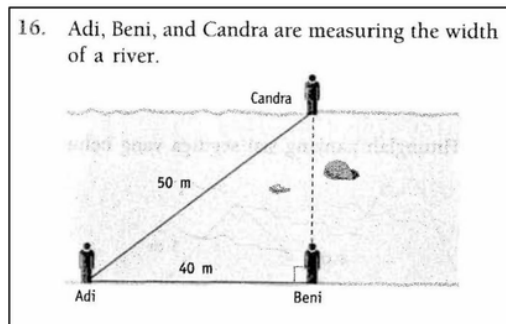


Figure 2. An example of *transformation error*

As a further endeavor to improve students' performance, the CoMTI project focused on identifying possible reasons for students' errors. For this purpose, opportunity-to-learn

was considered as the key concept. Students' opportunity-to-learn to solve context-based tasks were investigated from two aspects: textbooks and teachers' teaching practices. Wijaya, Van den Heuvel-Panhuizen, and Doorman (2015) analyzed Indonesian mathematics textbooks and, in general, found a low quantity of context-based tasks in the textbooks. This result give an early indication about insufficient opportunity-to-learn to solve context-based tasks offered in Indonesian textbooks. To get a better understanding of the relation between students' errors and the textbooks, Wijaya et al. conducted a further investigation into the characteristics of context-based tasks in the textbooks in which they found correspondences between these two aspects. The substantial number of students' comprehension errors corresponds to the high number, i.e. 85%, of context-based tasks that provide only relevant information and, therefore, do not require students to select information. The high number of transformation errors made by students relates to a low number of context-based tasks with relevant and essential contexts. Furthermore, all context-based tasks are located after the explanation sections in which a particular mathematics topic is discussed. It means students do not get enough opportunity to identify the procedures required to solve the tasks. These results indicate that one of strategies that can be used to improve students' performance on context-based tasks is by developing textbooks, i.e. providing more context-based tasks which: (i) use essential and relevant context, (ii) include irrelevant information, and (ii) do not provide the required procedure(s) explicitly.



**Figure 3.** A task in Indonesian mathematics textbook that provides only the relevant information and clearly indicates the required procedure

Students' opportunity-to-learn was also investigated from teachers' teaching practices for which Wijaya, Van den Heuvel-Panhuizen and Doorman (submitted) examined teachers' teaching approach and the types of context-based tasks offered by teachers in their classroom practices. Wijaya et al. found that the teachers' teaching practices did not offer enough opportunity for students to learn to solve context-based tasks. The teachers mainly used directive teaching approach in which they tended to directly explain and give instruction. Such practice was in contrast to the practice recommended by experts in modeling (e.g. Blum, 2011) that context-based tasks should be taught through a student-centered and investigative teaching approach in which students are actively involved and the teacher's role is consultative rather than directive. With respect to the characteristics

of tasks offered by the teachers in their teaching practices, the teachers mainly give tasks that provide only the relevant information and have explicit procedure. Such tasks do not support students to learn to select relevant information and to identify required procedure. These results provide important basis for developing ways to improve students' performance on context-based tasks, i.e. by improving teachers' teaching practices from two aspects: using consultative teaching and providing more context-based tasks which include irrelevant information and has missing information.

The final phase of CoMTI was developing an intervention program based on the results of the error analysis and the investigation into opportunity-to-learn (Wijaya, Van den Heuvel-Panhuizen, & Doorman, submitted). This intervention program comprised two components: consultative teaching approach and a set of context-based tasks that include irrelevant information and do not provide the required procedures explicitly. A closer examination of the effect of the intervention on students' errors revealed a significant difference between the experimental group and the control group for the decrease in the total number of errors ( $\chi^2(1, n = 4127) = 4.149, p = .042$ ). This finding reflects a positive influence of intervention program on reducing students' errors. In particular for transformation errors a positive influence was found only for context-based tasks addressing graphs, i.e. the topic taught during the intervention period. Reflecting upon this finding, it can be learned that to improve students' ability to identify the required procedure it is essential to provide 'mixed' context-based tasks, i.e. tasks that are related to the topic being taught and also other topics.

### Final Remarks

The aforementioned discussion and the example from CoMTI project show the importance of error analysis and an investigation into opportunity-to-learn as preliminary steps to develop an appropriate innovation, i.e. an innovation that fits the needs and the characteristics of a particular country. By connecting students' errors or difficulties with opportunity-to-learn, we could identify what competences to be developed and what is missing in the existing educational process. However, we still have to consider iterative analysis and redesign aspects of design research (see Wang & Hannafin, 2005). For example, a reflection upon the Wijaya et al.'s (submitted) finding that their intervention program has a better effect, in terms of transformation errors, for tasks addressing the taught topic indicates a room for improvement, such as providing context-based tasks addressing various topics.

### Note:

The appendix shows a summary how an intervention program was developed on the basis of error analysis and an investigation into opportunity-to-learn.

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Appendix

STUDENTS' DIFFICULTIES (Study 1)

**Analysis of Indonesian students' errors when solving context-based tasks**

The most dominant error types:

- comprehension errors; in particular, errors in selecting relevant information.
- transformation errors; in particular, errors identifying the required mathematical procedures.

OTL AS A KEY CONCEPT FOR STUDENTS' DIFFICULTIES: POSSIBLE REASONS (Study 2 and Study 3)

**Analysis of Indonesian mathematics textbooks**

- Exposure of the context-based tasks:
  - Only about 10% of all tasks were context-based.
- Characteristics of the context-based tasks:
  - most of the tasks used *camouflage contexts* and provide explicit indications about the required mathematical procedures.
  - most of the tasks provide *matching information*, i.e. only the information that is needed to solve the tasks.
  - almost no *reflection tasks*, i.e. tasks with highest cognitive demands which require constructing original mathematical approaches and communicating complex arguments and complex reasoning.

**An investigation into Indonesian mathematics teachers' teaching practices**

Teachers' report about the characteristics of context-based tasks offered to students:

- most of the teachers frequently give tasks with *explicit procedures*
- most of the teachers frequently give tasks with *matching information*
- a half of the teachers never or rarely give tasks with *superfluous information*
- a half of the teachers never or rarely give tasks with *missing information*.

Teachers' teaching approach:

- Over all stages of solving context-based tasks:
  - No instruction was given in 42% of all questions discussed in the lessons.
  - Directive teaching was applied in 47% of all questions discussed in the lessons.
  - Consultative teaching was applied in only 12% of all questions discussed in the lessons.

Specified for the stages of solving context-based tasks:

- Directive teaching was most frequently applied in the comprehension and the transformation stages.
- Consultative teaching was mostly applied in the mathematical processing stage.
- Almost no attention was paid to the encoding stage.

OTL AND STUDENT PERFORMANCE (Study 4)

Offering students opportunity-to-learn (OTL)		Effects of the OTL on students' performance
<p><b>Context-based tasks:</b></p> <ul style="list-style-type: none"> <li>- Context-based tasks with missing or superfluous information.</li> <li>- Context-based tasks with a relevant context that requires modeling</li> <li>- Context-based tasks with non-explicit procedure</li> </ul>	<p><b>Consultative teaching approach with metacognitive prompts:</b></p> <ul style="list-style-type: none"> <li>- Paraphrasing: asking students to formulate a task in their own words.</li> <li>- Underlining all information and circling only the relevant information</li> <li>- Self-questioning, e.g. "Do we have enough information to solve the task?"</li> <li>- Self-questioning, e.g. "If that are possible strategies to solve the task?"</li> </ul>	<ul style="list-style-type: none"> <li>- A positive effect of the OTL on students' task comprehension was found:                             <ul style="list-style-type: none"> <li>- Students could understand better the instruction of the task</li> <li>- Students' ability to select relevant information improved</li> </ul> </li> <li>- In general no effect of the OTL on students' ability to transform a real-world problem into a mathematical problem. However, a positive effect was found for tasks addressing an interpretation of a graph, which in fact was related to the topic taught during the intervention.</li> <li>- This finding leads to a recommendation to offer students 'mixed exercises', i.e. a set of context-based tasks that address various topics.</li> </ul>

# Key ingredient

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